



- (A)  $\frac{1}{10} \sinh 3x$  (B)  $\frac{1}{5} \cosh 3x$  (C)  $\frac{1}{10} \cosh 3x$  (D) none of these
- i)  $\frac{1}{D-a} X$ , (where  $X = k$  is constant) equal to  
 (A)  $-\frac{k}{a}$  (B)  $\frac{k}{a}$  (C)  $ka$  (D)  $-ka$
- j) Eliminating the arbitrary constants,  $a$  and  $b$  from  $z = (x+a)(y+b)$ , the partial differential equation formed is  
 (A)  $z = \frac{p}{q}$  (B)  $z = p+q$  (C)  $z = pq$  (D)  $xq = yp$
- k) The general solution of the equation  $p \tan x + q \tan y = \tan z$  is  
 (A)  $F\left(\frac{\cos x}{\cos z}, \frac{\cos y}{\cos z}\right) = 0$  (B)  $F(\sin x \sin y, \sin x + \sin y) = 0$   
 (C)  $F\left(\frac{\sin y}{\sin x}, \frac{\sin z}{\sin x}\right) = 0$  (D) none of these
- l) Particular integral of  $(D^2 - D^2)z = \cos(x+y)$  is  
 (A)  $\frac{x}{2} \cos(x+y)$  (B)  $x \sin(x+y)$  (C)  $x \cos(x+y)$  (D)  $\frac{x}{2} \sin(x+y)$
- m) The order of convergence in Bisection method is  
 (A) zero (B) linear (C) quadratic (D) None of these
- n) The criterion for convergence for solving  $f(x) = 0$  by the Newton-Raphson method is  
 (A)  $\left| \{f'(x)\}^2 \right| > |f(x) \cdot f''(x)|$  (B)  $\left| \{f'(x)\}^2 \right| < |f(x) \cdot f''(x)|$   
 (C)  $\left| \{f'(x)\}^2 \right| = |f(x) \cdot f''(x)|$  (D) none of these

**Attempt any four questions from Q-2 to Q-8**

- Q-2 Attempt all questions (14)**
- a) Using Newton-Raphson method, find the root of  $f(x) = \sin x + \cos x$  correct to three decimal places. (5)
- b) One real root of the equation  $x^3 - 4x - 9 = 0$  lies between 2.625 and 2.75. Find the root using Bisection method. (5)
- c) Evaluate:  $L(te^{-4t} \sin 3t)$  (4)
- Q-3 Attempt all questions (14)**
- a) Show that  $x^2 = \frac{\pi^2}{3} + 4 \sum_{n=1}^{\infty} (-1)^n \frac{\cos nx}{n^2}$  in the interval  $-\pi \leq x \leq \pi$ . Hence deduce that  $\frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \dots = \frac{\pi^2}{12}$ . (5)
- b) Find the Fourier series for (5)



$$f(x) = a(x-l), \quad -l < x < 0$$

$$= a(l+x), \quad 0 < x < l$$

and deduce that  $1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots = \frac{\pi}{4}$ .

- c) Given that one root of the equation  $x^3 - 4x + 1 = 0$  lies between 1 and 2. Find the root correct to 3 significant digits using Secant method. (4)

**Q-4**

**Attempt all questions** (14)

- a) Using Laplace transform method solve: (5)

$$\frac{d^2x}{dt^2} + 2\frac{dx}{dt} + 5x = e^{-t} \sin t, \quad x(0) = 0, \quad x'(0) = 1$$

- b) Using convolution theorem, evaluate  $L^{-1} \left\{ \frac{s}{(s^2 + 4)^2} \right\}$ . (5)

- c) Solve:  $\frac{\partial^2 z}{\partial x^2} = a^2 z$  given that when  $x = 0$ ,  $\frac{\partial z}{\partial x} = a \sin y$  and  $\frac{\partial z}{\partial y} = 0$ . (4)

**Q-5**

**Attempt all questions** (14)

- a) Evaluate:  $L^{-1} \left[ \frac{1}{s^3 - a^3} \right]$  (5)

- b) Solve:  $(D^2 - 2D + 1)y = xe^x \sin x$  (5)

- c) Solve:  $pz - qz = z^2 + (x + y)^2$  (4)

**Q-6**

**Attempt all questions** (14)

- a) Solve:  $D^2(D^2 + 4)y = 48x^2$  (5)

- b) If  $f(x) = \begin{cases} x & , 0 < x < \frac{\pi}{2} \\ \pi - x & , \frac{\pi}{2} < x < \pi \end{cases}$  then show that (5)

$$f(x) = \frac{4}{\pi} \left( \frac{\sin x}{1^2} - \frac{\sin 3x}{3^2} + \frac{\sin 5x}{5^2} - \dots \right).$$

- c) Solve:  $L \left( \frac{e^{-at} - e^{-bt}}{t} \right)$  (4)

**Q-7**

**Attempt all questions** (14)

- a) Solve by the method of variation of parameters:  $\frac{d^2y}{dx^2} + a^2y = \sec ax$  (5)

- b) Solve:  $x^3 \frac{d^3y}{dx^3} + 2x^2 \frac{d^2y}{dx^2} + 2y = 10 \left( x + \frac{1}{x} \right)$  (5)

- c) Solve:  $\frac{\partial^2 z}{\partial x^2} - 4 \frac{\partial^2 z}{\partial y^2} = \cos 2x \cos 2y$  (4)

**Q-8**

**Attempt all questions** (14)

- a) The following table gives the variations of periodic current  $i = f(t)$  amperes over a period  $T$  sec. (7)



|             |      |               |               |               |                |                |      |
|-------------|------|---------------|---------------|---------------|----------------|----------------|------|
| $t$ (sec) : | 0    | $\frac{T}{6}$ | $\frac{T}{3}$ | $\frac{T}{2}$ | $\frac{2T}{3}$ | $\frac{5T}{6}$ | $T$  |
| $i$ (A) :   | 1.98 | 1.30          | 1.05          | 1.30          | -0.88          | -0.5           | 1.98 |

Show, by harmonic analysis, that there is a direct current part of 0.75 amp. in the variable current and obtain the amplitude of the first harmonic.

- b) Using the method of separation of variables, solve  $\frac{\partial u}{\partial x} = 2 \frac{\partial u}{\partial t} + u$ , (7)  
 given  $u(x, 0) = 6e^{-3x}$

